

Calculus with Analytic Geometry II

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1 Sequences/Series Worksheet

I. Find function representation of the following sequences. For each sequence, determine whether it converges or diverges. If it converges, find its limiting value and prove it using $\epsilon - N$ definition.

a. $\frac{1}{2}, -\frac{2}{3}, \frac{3}{4}, -\frac{4}{5}, \dots$

b. $1, 3, 5, 7, \dots$

c. $\frac{1}{3}, \frac{2}{5}, \frac{3}{7}, \frac{4}{9}, \dots$

II. For each series, determine if the sequence of partial sums converges or diverges. If it converges, find its limiting value (you may use L'Hopitals rule).

a. $\sum_{k=0}^{\infty} \frac{1}{3^k}$

b. $\sum_{k=2}^{\infty} \frac{1}{k^2 - 1}$

c. $\sum_{k=1}^{\infty} \frac{1}{k}$